STRATEGIC GAME THEORY

www.agsm.edu.au/bobm/teaching/SGTM.html

Outline of the course:

Lecture	Topic
	I Foundations
1	Introduction and General Principles
2, 3	Simultaneous-Move Games I
4	Games with Sequential Moves
5	Simultaneous-Move Games II
6	Combining Sequential and Simultaneous

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7-10	Decision Analysis: Games Against Nature

11	III Broad classes of games and strategies Mixed Strategies and Unpredictability
12, 13	Uncertainty and Information
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15, 16	The Prisoner's Dilemma and Repetition

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	V
22, 23	Student presentations

Dixit A., & Skeath S., Games of Strategy, New York: Norton: 2nd edition, 2004.

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Dixit A., & Nalebuff B., Thinking Strategically: the Competitive Edge in Business, Politics, and Everyday Life, New York: Norton, 1991. (and their follow-up, The Art of Strategy, 2008)

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Bierman H.S. & Fernandez L., Game Theory with Economic Applications, Addison-Wesley, 2nd ed., 1998.

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And the Game Theory Society at www.gametheorysociety.org

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Attend lectures and participate

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- Write an imaginative Term Project.
- See a list of examples of excellent past projects at the back of the Course Outline. Email me for soft copies.

Question: Low Price or High Price?

You can choose Low or High Price:

Profits:

Low Price High Price
You \$40 m \$80 m

Question: Low Price or High Price?

You can choose Low or High Price:

Profits:

Low Price High Price

You \$40 m \$80 m

Rival \$20 m \$160 m

(Write down your answer.)

Further ...

Further ...

What if "Harm"?:

	Low Price	High Price
You	\$40 m	\$80 m
Rival	-\$100 m	\$40 m

The Moral?

Quotable Quotes — Game Theory:

"When government auctioneers need worldly advice, where can they turn? To mathematical economists, of course ... As for the firms that want to get their hands on a sliver of the airwaves, their best bet is to go out first and hire themselves a good game theorist."

The Economist, July 23, 1994, p.70.

the "most dramatic example of game theory's new power ... It was a triumph, not only for the FCC and the taxpayers, but also for game theory (and game theorists)."

Fortune, February 6, 1995, p.36.

"Game theory, long an intellectual pastime, came into its own as a business tool."

Forbes, July 3, 1995, p.62.

Game Theory

**Conventional economics takes the structure of markets as fixed. People are thought of as simple stimulus-response machines. Sellers and buyers assume that products and prices are fixed, and they optimize production and consumption accordingly. Conventional economics has its place in describing the operation of established, mature markets, but it doesn't capture people's creativity in finding new ways of interacting with one another.

But ...

World. In game theory, nothing is fixed. The economy is dynamic and evolving. The players create new markets and take on multiple roles. They innovate. No one takes products or prices as given. If this sounds like the free-form and rapidly transforming marketplace, that's why game theory may be the kernel of a new economics for the new economy.

- Brandenburger & Nalebuff Foreword to Co-opetition

Strategic Decision Making

Business is war and peace.

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Co-opetition

(See Lectures 20 & 21 later and Brandenburger & Nalebuff in the Package.)

Manual for "Co-opetition"

How to:

- cooperate without being a saint
- compete without killing the opposition.
- Game Theory

A Case: The New York Post v. the New York News

> Rupert Murdoch's New York Post takes on the New York Daily News.

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	N.Y. Post	N.Y. News
January 1994	40¢	40¢
February 1994	50¢	40¢
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July 1994	50¢	50¢

What happened?

Until Feb 1994 both papers were sold at 40¢. Then the *Post* raised its price to 50¢ but the *News* held to 40¢ (since it was used to being the first mover).

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So in March the *Post* dropped its Staten Island price to 25¢ but kept its price elsewhere at 50¢, until *News* raised its price to 50¢ in July, having lost market share in Staten Island to the *Post* and having accepted that the *Post* would henceforth be the leader in any price hike.

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So both were now priced at 50¢ everywhere in NYC.

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So game theory provides a framework for an everrapidly changing world.

Players: customers, suppliers, rivals, allies; Change any, including yourself.

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- Added Values: what each player adds to the game (taking the player out would subtract their added value).

 Ways to raise yours, or lower theirs.
- Rules: give structure to the game; in business no universal set of rules from law, custom, practicality, or contracts Can revise exiting rules, or devise new ones.

More PARTS ...

Tactics: moves to shape the way:

- players perceive the game, and hence
- how they play

Tactics to reduce misperception, or to create or maintain misperception.

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PARTS does more than give a framework, it also provides a complete set of levers.

PARTS provides a method to promote non-routine thinking.

Wider issues.

In Lectures 20 & 21 we go beyond the more micro issues \rightarrow wider issues:

Which game should your firm/organisation be in?

It's no good sticking to your knitting if there's no demand for jumpers.

There we elaborate on the five PARTS, and introduce the Value Net.

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Which tyre?

Write down.

Piemax Inc. bakes and sells dessert pies.

Its decision:

- price high or low for today's pies?

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A naïve option:

simply optimise its pricing policy given its beliefs about rivals' prices, or . . .

Think strategically...

Alternative:

try to predict those prices,

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Game Theory \rightarrow

- Piemax should build a model of the behaviour of each individual competitor,
- Which behaviour would be most reasonable to expect?

Issues for Later

Later: what is an equilibrium?

Later: ought Piemax to believe that the market outcome \rightarrow equilibrium?

Now: what kind of model?

The simplest kind of model.

- All bakers operate for one day only (a so-called one-shot model)
- All bakers know the production technologies and objectives of the others
- Study with the tools of:
 - > payoff matrix games and
 - > Nash equilibrium

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John Forbes Nash's Equilibrium.

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A single Nash equilibrium is not necessarily the outcome of the game (see the Chicken! Game, with two N.E. below).

Repeated interactions.

If more than one day (a repeated game or interaction):

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- e.g. low price today may:
 - ightarrow customers switch from a rival brand
 - → increase Piemax' market share in the future
- e.g. baking a large batch of pies may
 - → allow learning by doing by the staff
 - & lower production costs in the future.

But there are dangers in cutting its price!

Its rivals may be influenced by Piemax's price today

- → a low Piemax price may trigger
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Such dynamic games can be analysed using:

- extensive-form game trees and
- the solution concept of subgame perfection

Later: Subgame Perfect Equilibrium: a Nash equilibrium that does not rely on non-credible threats (that satisfies backwards induction).

How about information?

- What if Piemax is uncertain of the cost functions or the long-term objectives of its rivals?
 - Has Cupcake Pty Ltd just made a breakthrough in large-batch production?
 - Does Sweetstuff plc care more about market share than about current profits?
 - And how much do these rivals know about Piemax?

Incomplete information games.

Acting in a fog: perceptions rule!

And learning?

- > If the industry continues for several periods, then Piemax ought to learn about Cupcake's and Sweetstuff's private information from their current pricing behaviour and use this information to improve its future strategy.
- ➤ In anticipation, Cupcake and Sweetstuff may be loath to let their prices reveal information that enhances Piemax's competitive position:
- > They may attempt to manipulate Piemax's information, by their actions etc.

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And vice versa.

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- Strategic situations:

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Look forward and reason backwards!

 a procurement manager trying to induce a subcontractor to search for cost-reducing innovations

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- how low to bid for a government procurement contract

- how high to bid in an auction

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- the haggling between a buyer and seller of a used car
- collective bargaining between a trade union/employees and an employer

Games v. Decisions

Decisions:

no strategic elements, just uncertainty (Lectures 6-10)

Games:

mutual awareness of the interactive effects; head-to-head interactions of 2 or a few players or

mutual commitment and private information; from competitive market to bilateral relationship

e.g. credit and insurance markets

Classifying Games

- > Sequential or Simultaneous? (L 2, 3, 4, 5)
- > Total Conflict or Some Commonality?
- > Once-Off or Repeated? (L 15, 16)
- > Full or Asymmetric Information? (L 12, 13)
- > Rules Fixed or Changeable? (L 20, 21)
- > Agreements to Cooperate Enforceable?

Terminology and Assumptions

- > Strategies, actions
- > Payoffs, not just \$
- > Rationality (not selfishness), know one's self
- Common Knowledge, I know that you know that I know that ...
- > Equilibrium, no regrets
- > Dynamics and Evolutionary Games, repetition
- > Observation and Experiment, experiments