# Lecture 19: Contracting, or The Rules of the Game, or Mechanism Design

(See McMillan, Chap. 8 & 9, and DixitSkeathReiley Chap. 14)

#### **Topics:**

- I. Strategising versus Economising
- 2. Using Game Theory to Enhance Efficiency
- 3. Creating Incentives
- 4. Designing Contracts
- 5. Application to Financial Contracts

# 1. Strategising versus Economising

#### Strategising ...

(See Williamson's paper in the Package: he shared the Nobel prize in 2009, for "analysis of economic governance, especially the boundaries of the firm".)

Game Theory is usually applied to issues of "strategising", i.e., beating rivals or consumers:

- > Pre-emptive threats/entry deterrence.
- > Cartel enforcement.
- > Bargaining and bidding.

#### ... versus Economising

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- Illusion from micro theory that it's easy to minimise costs: set Wage = Value of the Marginal Product of Labour.
  - But this is very difficult and costly to monitor on the shop floor.
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- 2. Illusion that powerful tools from game theory don't help to economise, in Finance or in Human Resource Management.

But game theory can be very useful, especially for economising.

#### Contracts Integrate ...

# Contracts integrate game theory and standard microeconomics:

- > A contract: an agreement that supports exchange between supplier (seller) and buyer (demander).
- > Standard microeconomics: Supply = Demand (and produce where Marginal Cost = Price) is just the Nash equilibrium of a game where no-one's decisions affect the welfare of anyone else. (Perfect competition, and all are price-takers.)
- > Costless contracts: Even with small numbers, we can achieve the perfect competition outcome.

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- I. Predicts (or analyses) what will happen under different contractual arrangements. What are the incentives?
- 2. Allows us to choose (or to design) the best one, (Choosing the Game).
  e.g.:
  - Make or Buy? (production integration)
  - Debt or Equity? (capital structure)
  - Privatised or Publicly Owned? (ownership)
  - Division or Spin Off? (organisational structure)

# 2. Using Game Theory to Enhance Efficiency

#### **General Principles**

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#### **General Principles**

- I. Game theory is often taught via simple examples, chosen on an ad-hoc basis. e.g. battles, interactions, kids and credibility.
- 2. The Contracting perspective, by contrast, is:
  - > choose the rules of the game, the contract,
  - > solve (or simulate) for the equilibrium of this game, of this contract,
  - > then ask:
    - are the players pleased with the outcomes?
    - what could they do to achieve a better outcome? How?

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- e.g. employment contract pay, conditions, work, supervisor's interests, etc;
- e.g. financing contract
- e.g. franchise contract
- e.g. outsourcing contract

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- Q: How can you create appropriate incentives?
- A: Rewards & punishments carrots & sticks.
- > The pervasive Principal-Agent problems:
  - author v. publisher
  - debt v. equity
  - landlord v. tenant
  - subcontractor v. price contractor
  - employer v. employee
  - insured v. insurer

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  - insured v. insurer
- ➤ Whereas HRM: change the Agent's goals → the Principal's goals, now on the contrary ...
- Here: we focus on the use of monetary rewards important (although not necessary) and simple to understand.

#### Piece Rates, Commissions, & Royalties

#### Performance incentives are ubiquitous —

- piece rates/bonuses/commissions for production workers
- pay for performance (bonuses, share options)
- sales representatives paid by commission
- professional sports? (tournaments, winner-takesmost)
- academic salary supplements
- forecasters' pay ∞ accuracy (?)

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# Contracts can also be used in cost minimisation instead of maximum output:

- > cost-minimisation is costly
- > contracts vary from one extreme to another who bears the risk? The Principal or the Agent?
  - fixed-price contracts?
  - cost-plus contracts?
  - incentive contracts?

A verbal contract isn't worth the paper it's written on.

— Samuel Goldwyn

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- OK if constant, predictable relationship:
   Agent's effort ⇒ Agent's performance
- but random events, uncertainties intervene
   i.e. the Agent may be unlucky or lucky.
- the Agent may "slack" or "shirk"

#### Principals' and Agents' interests may diverge.

- So: 1. Divergence of interests.
  - 2. Imperfectly observable "efforts" of the Agent.
    - not necessarily how hard the Agent works
    - but to what end does the Agent toil? (profits, or size, etc.?)

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The incentive effect — is at the margin,

where costs of extra effort = gain to the Agent
from extra effort.

The higher the commission rate  $\lambda$ , then the greater the Agent's selling effort.

#### Carrots & Sticks

# Look at from the worker's (the Agent's) point of view:

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#### Ideally the Principal would like to set:

> Piece rates or commission as a continuum:

$$\frac{\Delta \text{ reward}}{\Delta \text{ performance}} > 0$$
 where performance is measurable.

#### But incentive schemes can distort behaviour.

> They are often discontinuous:

$$\frac{\Delta \text{ reward}}{\Delta \text{ performance}} = 0 \text{ or } \frac{\Delta \text{ punishment}}{\Delta \text{ performance}} = 0$$

- threat of firing, loss of contract
- fines
- legal liabilities
- prizes, promotions, bonuses

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- threat of firing, loss of contract
- fines
- legal liabilities
- prizes, promotions, bonuses
- > But discontinuous incentive schemes can substitute for continuous:
  - wage (\$/hr) + punishment after monitoring (firing)
  - wage (\$/hr) + reward after monitoring (promotion)

#### **Multi-Dimensional Performance**

#### A danger:

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#### One tradeoff: Quality

- quantity v. quality
   e.g. jet engine blades
   e.g. production-line workers,
   "shirking" = higher defect rates
- when quality is hard to monitor
   e.g. solution: pay all but the quality-control
   workers by the piece, since it is difficult to control
   the quality of quality control (:-)

#### Moral hazard might be suspected

 even with time payment, the Principal can use discontinuous rewards/punishments to mimic continuous incentive schemes.

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- even with time payment, the Principal can use discontinuous rewards/punishments to mimic continuous incentive schemes.
- e.g. Sears ended its commissions to its mechanics (the Agents), to enhance its credibility with its customers, who suspected over-servicing of their cars as a result of the mechanics' incentives.

Sears' mechanics became regular employees, paid by the week.

#### The Principal's Ideal Payment Scheme

"The shortest and best way to make your fortune is to let people see clearly that it is in their interests to promote yours."

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Q: But how?

A:

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Q: But how?

A: The Principal sets the Agent's marginal payment scheme  $\lambda$  (commission, royalty, piece rate, etc.) at 100%.

#### **Example: the salesperson example:**

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- Q: What is the ideal amount of the Agent's effort, from the Principal's viewpoint?
  - Assume the Agent's costs equal the Principal's;
     and assume diminishing return to effort.
- If the Principal acted alone, then she would get 100% of the benefits and incur 100% of the costs. So the Principal would exert effort to the point where marginal costs equal marginal returns or effort: marginal cost (effort) = marginal returns (P = MC?)
- When the Agent acts, he bears the full cost of any marginal effort, whatever the commission rate  $\lambda$ .

#### Optimal commission? How to raise money?

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- Thus  $\lambda = 100\% \Rightarrow$  the Agent's interests and the Principal's are identical, and the gain from trade to be divided between the Principal and the Agent is maximised.
- Q: But with  $\lambda = 100\%$ , how does the Principal earn anything from the deal?

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- .. In effect the Principal sells the Agent the right to be the Agent: self-employed, arm's-length relationship.
- e.g. Lord Cornwallis in Bengal, in the late 18th century, sold the right to collect taxes to private individuals, (who were hated).

## 4. Designing Contracts

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- 2. the Agent's performance is a function of outside events, with the Agent bearing all of the risk but if the Agent is risk averse, it may not be in the Principal's interest to force the Agent to bear the risk.

#### **Contracting with Private Information**

e.g. The sales manager (the Principal) knows only that the value of a particular area is either high or low, but only the salesperson (the Agent) knows which.

Possible for the manager to offer the Agent a different package (commission rate  $\lambda$  < 100% and base salary B) depending on whether the Agent reports his sales potential as high or low, subject to the Agent's fallback position.

Accountability for what they report?

#### **Honesty?**

Possible (with appropriate packages — see McMillan Ch. 9) to induce the Agent to give an honest report:

- > Total package payments must be higher when the potential is correctly reported as high than when correctly reported as low.
- > Commission rate  $\lambda$  must be higher, and the base salary B lower, for a report of high potential than for a report of low potential.

#### How well does the Principal do?

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#### The commission rate $\lambda$ must do double duty:

- elicit information, and
- 2. elicit effort (as above)
- : it must be less than 100%,
- the Agent's private information costs the Principal.

(We saw a similar cost when Sally tried to screen Burt, in Lecture 12.)

Useful to use salespeople's information in contracts and in corporate planning.

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- I. self-selection: more skillful workers choose companies with piece-rate payments, while others prefer fixed salaries;
- 2. incentives: people work harder when rewarded for the results of their extra effort;
- 3. since piece-rate workers' pay is not only higher but more volatile than fixed-wage workers' pay, to some extent the higher earnings are compensation for higher risk borne by the piece-rate workers.

#### **Risk-Sharing versus Incentives**

Performance-based contracts subject the Agents to risk.

Most people are risk-averse: insure against risk by forgoing some of their anticipated earnings.

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... We might expect a smaller average payment to the Agent in return for the Principal absorbing some of the risk.

But this will weaken the Agent's incentives:

NB: Any contract will be a compromise between risk-bearing and incentives.

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The commission rate  $\lambda$  should depend on the relative size of these two numbers.

So long as the Principal is less risk-averse than the Agent, sharing risk is a win-win proposition.

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An incentive contract is an intermediate form: allows the Agent to pass on some fraction of added cost as a higher price to the Principal.

#### **Relative Performance Evaluation**

With perfect information, in order to infer the Agent's actions, the Principal could design a contract to elicit the desired actions.

The Principal can obtain more information than just the Agent's output: the outputs of others.

This can be obtained through benchmarking with other firms, or though tournaments among Agents, with prizes and rewards.

(See McMillan Ch. 10 on Setting Executives' Incentives.)

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#### I. Fundamentals:

- > The Entrepreneur (the Principal) has a risky project that costs \$1 million to start.
- > It pays: \$10 million with probability = 3/4 \$0 with probability = 1/4
- Investors (Agents) are risk-neutral; and the market interest rate is 0% p.a.

Hence, expected NPV = 
$$\$10 \times \frac{3}{4} + 0 \times \frac{1}{4} - \$1$$
  
=  $\$6.5 \text{ mn} > 0$ .

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The Entrepreneur gets  $(1 - \lambda) \times \frac{3}{4} \times 10 \le $6.5$  mn, the net wealth created.

#### ... and Debt Contracts

> Debt: The Entrepreneur promises to pay the first \$D dollars to Investors if a Success. Solving:

$$D \times \frac{3}{4} = 1$$
,  $\Rightarrow D = $1.33$  million

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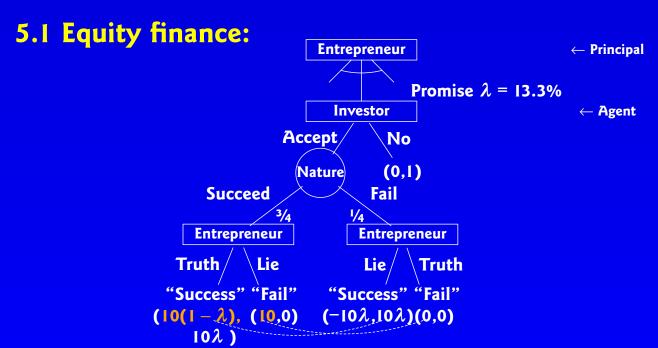
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Q: So why are most projects like this (large inside ownership) financed with debt?

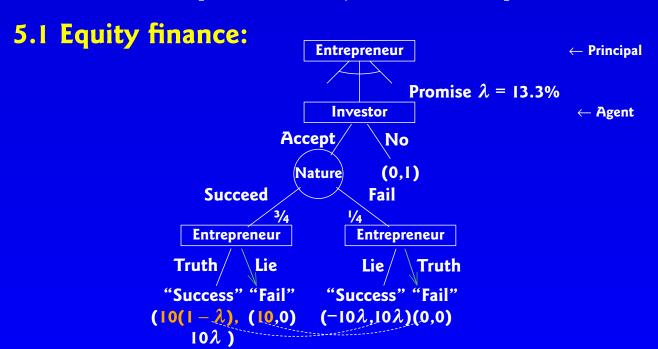
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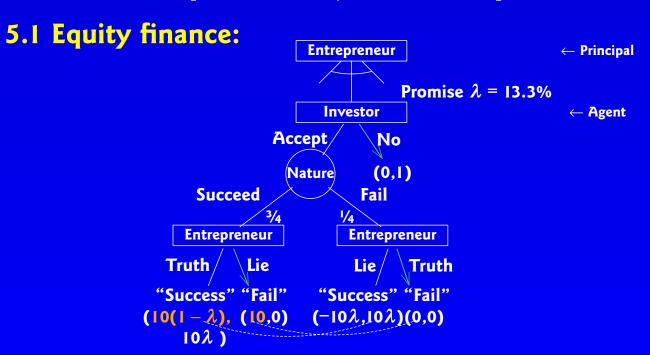


Fig 1: Equity Finance (Entrepreneur, Investor)

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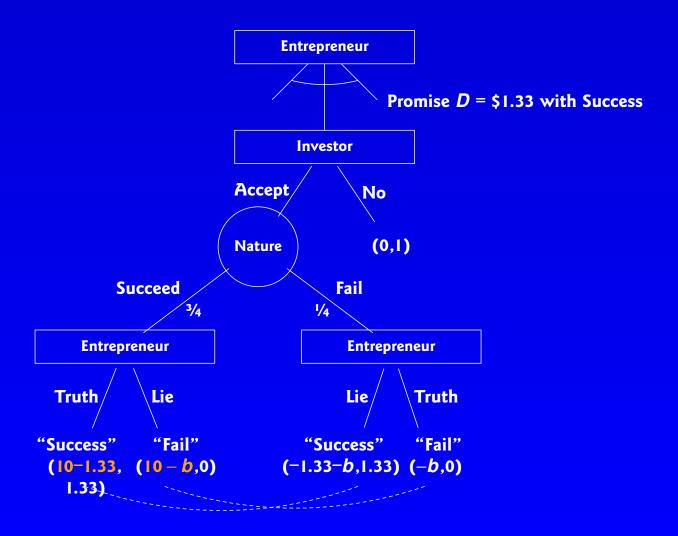


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- .. The Entrepreneur announces "Failure" in both cases:  $10 > 10(1-\lambda)$  (Probability 1)
- ∴ The Investor says No, no investment: because 1 > 0
- > Mutual tragedy inefficient.

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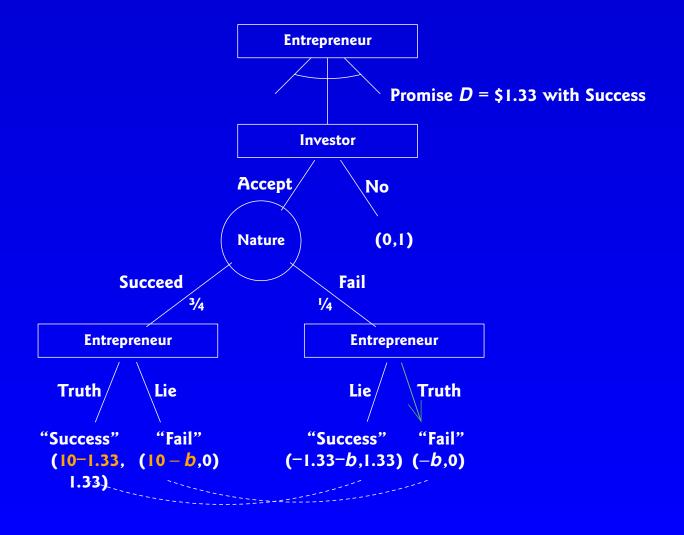


Fig 2: Debt Finance (Entrepreneur, Investor)

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More efficient, because dead-weight loss b.

Intermediaries?

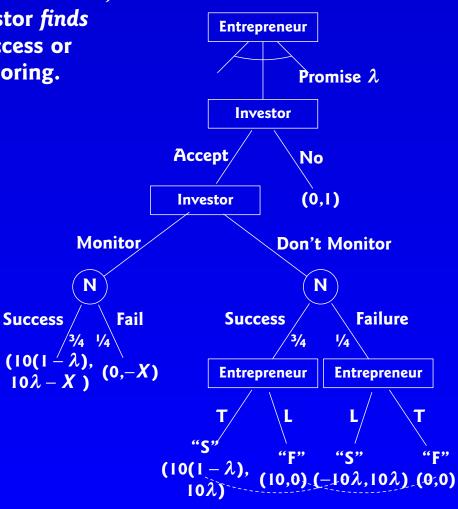
Large banks less often?

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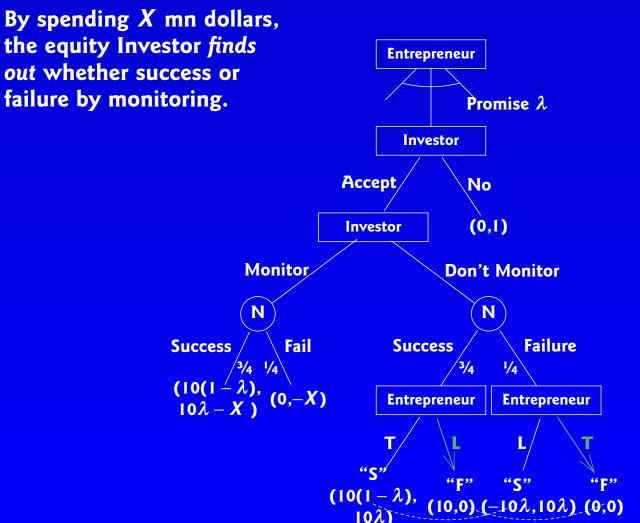


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### 5.4 Conclusion: Debt or Relationship?

Consider the return to the Entrepreneur in Fig 2. (with b = 1.33 mn to induce truth-telling) and in Fig 3:

then the Entrepreneur will choose Relationship Investing over Debt Finance if the expected return to her is higher for Relationship Investing than for Debt Finance, i.e., if:

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$$(1-\lambda) > \frac{3}{4} (10-1.33) - \frac{b}{4}$$

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Idea: to have sunk the monitoring cost X before knowing the outcome, then it's redundant if you find out it's successful.

But don't have to do messy ex-post bankruptcy.