Schelling, T. (1978). Micromotives and macrobehavior. New York: W. W. Norion (See especially 127-55.)

many lines and in many ways. There is segregation by sex, age, income, language, religion, color, personal taste, and the accidents of historical location. Some segregation results from the practices of organizations. Some is deliberately organized. Some results from the interplay of individual choices that discriminate. Some of it results from specialized communication systems, like languages. And some segregation is a corollary of other modes of segregation: residence is correlated with job location and ransport.

E blacks exclude whites from their church, or whites exclude blacks, the segregation is organized; and it may be reciprocal or one-sided. If blacks just happen to be Baptists and whites Methodists, the two colors will be segregated Surday morning whether they intend to be or not. If blacks join a black church because they are more comfortable among their own color, and whites ε white church for the same reason, undirected incividual choice can lead to segregation. And if the church bulletin board is where people advertise rooms for rent, blacks will rent rooms from blacks and whites from whites because of a communication system that is connected with churches that are correlated with color.

Some of the same nechanisms segregate college professors. The college rnay own some housing, from which all but college staff are excluded. Professors choose housing commensurate with their incomes, and houses are clustered by price while professors are clustered by income. Some professors prefer an academic neighborhood; any differential in professorial density will cause them to converge and increase the local density, and attact more professors. And house-hunting professors learn about available housing from colleagues and their spouses, and the houses they learn about are naturally the ones in neighborhood where professors already live.

commission to desegregate academics. Professors are not much missed by those they escape from in their residential choices. though proportionately concentrated, are usually a minority in their neighborhood. While indeed they escape classes of They are not much noticed by those they live among, and, people they would not care to live among, they are more conactive choice is more like congregation than segregation, scious of where they do live than of where they don't, and the though the result may not be so different. The similarity ends there, and nobody is about to propose a

behavior. By "discriminatory" I mean reflecting an awareness, tion, or sorting-that can result from discriminatory individual conscious or unconscious, of sex or age or religion or color or whatever the basis of segregation is, an awareness that influences decisions on where to live, whom to sit by, what occupatien to join or to avoid, whom to play with, or whom to talk to. It examines some of the individual incentives and individual perceptions of difference that can lead collectively to segregation. It also examines the extent to which inferences can be of individuals, the strengths of those preferences, and the acildrawn from actual collective segregation about the preferences This chapter is about the kind of segregation-or separa-

ities for exercising them. tinction he twofold, exhaustive, and recognizable. (Skin color, faculty. The only requirement of the analysis is that the disblacks, boys and girls, officers and enlisted men, students and distinction could constitute an interpretation-whites and States. The analysis, though is so abstract that any twofold of course, is neither dichotomous nor even unidimensional, but by convention the distinction is nearly twofold, even in the The main concern is segregation by "color" in the United

analysis. One is organized action-legal or illegal, coercive or United States census.) or malicious, moralistic or pragmatic. The other is the process, merely exclusionary, subtle or flagrant, open or covert, kindly At least two main processes of segregation are outside this

> rated from the rich, the less educated from the more educated, large y but not entirely economic, by which the poor get sepathe unskilled from the skilled, the poorly dressed from the well school with. Evidently color is correlated with income, and dressed-in where they work and live and eat and play, in income with residence; so even if residential choices were whom they know and whom they date and whom they go to whites and blacks would not be randomly distributed among color-blind and uncorstrained by organized discrimination,

the economically induced kind. Habit and tradition are substimotivated" segregation from the more organized kind or from residences. whether or not the fear is justified, and whether the sanctions tutes for organization. Fear of sanctions can coerce behavior tions can lead to concerted behavior. are consensual, conspiratorial, or dictated. Common expeda-It is not easy to craw the lines separating "individually

with discrimination. To choose a neighborhood is to choose neighbors. To pick a neighborhood with good schools, for schools. People may furthermore rely, even in making ecoexample, is to pick a neighborhood of people who want good rely on color as an index, adopt their signals and indices on color as an index of poverty or, believing that others believing that darker-skinned people are on the average poorer nemic choices, on information that is color-discriminating; than lighter-skinned, one may consciously or unconsciously rely The economically induced separation is also intermixed

cialized communication systems-especially distinct languages induced segregation are not clear lines at all. They are furtheraccordingly. ing with the three processes mentioned, is nevertheless a dif nore not the only mechanisms of segregation. Separate or spemotivated, the collectively enforced, and the economically -can have a strong segregating influence that, though interact-For all these reasons, the lines dividing the individually

SORTING AND MIXING: RACE AND SEX

Individucl Incentives and Collective Results

Economists are familiar with systems that lead to aggregate results that the individual neither intends nor needs to be aware of, results that sometimes have no recognizable counterpart at the level of the individual. The creation of money by a commercial banking system is one; the way savings decisions cause depressions or inflations is another.

Biological evolution is responsible for a lct of sorting and separating, but the little creatures that mate and reproduce and forage for food would be amazed to know that they were bringing about separation of species, territorial sorting, or the extinction of species. Among social examples, the coexistence or extinction of second anguages is a phenomenon that, though affected by decrees and school curricula, corresponds to no conscious collective choice.

Romance and marriage, as emphasized in Chapter 1, are exceedingly individual and private activities at least in this country, but their genetic consequences are altogether aggregate. The law and the church may constrain us in our choices, and some traditions of segregation are enomously coercive; but, outside of rcyal families, there are few marriages that are part of a genetic plan. When a short boy mairies a tall girl, or a blonds a brunette, it is no part of the individual's purpose to increase genetic andomness or to change some frequency distribution within the population.

Some of the phenomena of segregation may be similarly complex in relation to the dynamics of individual choice. One might even be tempted to suppose that some "unseen hand" separates people in a manner that, though foreseen and intended by no one, corresponds to some consensus or collective preference or popular will. But in economics we know a great many macro-phenomena, like depression and inflation,

crashes. What goes on in the "hearts and minds" of small savers has little to do with whether or not they cause a depression. The hearts and minds and motives and habits of millions of people who participate in a segregated society may or may not bear close correspondence with the massive results that collectively they can generate.

A special reason for doubting any social efficiency in aggregate segregation is that the range of choice is often so meager. The demographic map of almost any American metropolitan area suggests that it is easy to find residential areas that are all white or nearly so and areas that are all black or nearly so but hard to find localities in which neither whites nor nonwhites are more than, say, three-quarters of the total. And, comparing decennial maps, it is nearly impossible to find an area that, if integrated within that range, will remain integrated long enough for a couple to get their house paid for or their children through school.

Some Quantitative Constraints

Counting blacks and whites in a residential block or on a baseball team will not tell how they get along. But it tells something, especially if numbers and ratios matter to the people who are moving in or out of the block or being recruited for the team. With quantitative analysis there are a few logical constraints, analogous to the balance-sheet identities in economics. (Being logical constraints, they contain no news unless one just never thought of them before.)

The simplest constraint on dichotomous mixing is that, within a given set of boundaries, not both groups can enjoy numerical superiority. For the whole population the numerical ratio is determined at any given time; but locally, in a city or a neighborhood, a church or a school or a restaurant, either blacks or whites can be a majority. But if each insists on being a local majority, there is only one mixture that will satisfy

Relaxing the condition, if whites want to be at least three-fourths and blacks at least one-third, it won't work. If whites want to be at least two-thirds and blacks no fewer than one-fifth, there is a small range of mixtures that meet the conditions. And not everybody can be in the mixtures if the overall ratio is outside the range.

In spatial arrangements, like a neighborhood or a hospial ward, everybody is next to somebody. A neighborhood may be 10 percent black or white; but if you have a neighbor on either side, the minimum nonzero percentage of opposite color is 50. If people draw their boundaries differently we can have everybody in a minority: at dinner with men and women seated alternately, everyone is outnumbered two to one locally by the opposite sex but can join a three-fifths majority if he extends his horizon to the next person on either side.

Separating Mechanisms

The simple mathematics of ratios and mixtures tells us something about what outcomes are logically possible, but tells us little about the behavior that leads to, or that leads away from, particular outcomes. To understand what kinds of segregation or integration may result from individual choice, we have to look at the processes by which various mixtures and separations are brought about. We have to look at the incentives and the behavior that the incentives motivate, and particularly the way that different individuals comprising the society impinge on each other's choices and react to each other's presence.

There are many different incentives or criteria by which blacks and whites, or boys and girls, become separated. Whites may simply prefer to be among whites and blacks among blacks. Alternatively, whites may merely avoid or escape blacks and blacks avoid or escape whites. Whites may prefer the company of whites, while the blacks don't care. Whites

among whites, but if the whites can afford to live or to eat or to belong where the blacks cannot afford to follow, separation can occur.

Whites and blacks may not mind each other's presence, may even prefer integration, but may nevertheless wish to avoid minority status. Except for a mixture at exactly \$0:50, no mixture will then be self-sustaining because there is none without a minority, and if the minority evacuates, complete segregation occurs. If both blacks and whites can tolerate minority status but place a limit on how small the minority is—for example, a 25 percent minority—initial mixtures ranging from 25 percent to 75 percent will survive but initial mixtures more extreme than that will lose their minority members and become all of one color. And if those who leave move to where they constitute a majority, they will increase the majority there and may cause the other color to evacuate.

Evidently if there are lower limits to the minority status that either color can tolerate, and if complete segregation obtains initially, no individual will move to an area dominated by the other color. Complete segregation is then a stable equilibrium.

Sorting and Sciambling

Minor-league players at Dodgertown—the place where Dodger-affiliated clubs train in the spring—are served cafeteriastyle. "A boy takes the first seat available," according to the general manager. "This has been done deliberately. If a white boy doesn't want to eat with a colored boy, he can go cut ancibuy his own food. We haven't had any trouble."

Major-league players are not assigned seats in their dining hall; and though mixed tables are not rare, they are not the rule either. If we suppose that major- and minor-league racial attitudes are not strikingly different, we may conclude that

racial preference in the diring hall is positive but less than the price of the nearest meal.

Actually, though, there is an alternative: whites and blacks in like-colored clusters can enter the line together and, once they have their trays, innocently take the next seats alongside each other. Evidently they don't. If they did, some scrambling system would have had to be invented. Maybe we conclude, then, that the racial preferences, though enough to make separate eating the general rule, are not strong enough to induce the slight trouble of picking partners before getting food. Or perhaps we conclude that players lack the strategic foresight to beat the cafeteria line as a seat-scrambling device.

But even a minor-league player knows how to think ahead a couple of outs in deciding whether a sacrifice fly will advance the ball team. It is hard to believe that if a couple of players wanted to sit together it would not occur to them to meet at the beginning of the line; and the principle extends

when the mixture is lopsided. Joining a table with blacks and whites is a casual thing, but the mixture is lopsides are an exposed at the mixture is a casual thing, and being the seventh at a table with complete and the scious, or think that others are uncomfortable or self-conscious, or think that others are uncomfortable with blacks and whites is a casual thing, but being the seventh at a table with sciousness that spoils the easy atmosphere and can lead to complete and sustained separation

Hostesses are familiar with the problem Men and women mix nicely at stand-up parties until, partly at random and partly because a few men or women get stuck in a specialized conversation, some clusters form that are nearly all male or all female, selective migration then leads to the cocktail-partly equivalent of the Dodgertown major-league dining hall. Hostesses, too, have their equivalent of the cafeteria-line rule: they

alternate sexes at the dinner table, grasp people by the elbows and move them around the living room, or bring in coffee and make people serve themselves to disturb the pattern.

be segregated in the interest of safety; and an attempt is made and other enclosed public places; swimmers and surfess should usually good to segregate smokers from non-smokers in planes to keep slow-moving vehicles in the right-hand lane of traffic. smokers are raiely bothered by people who merely breather Many of these cichotomous groupings are asymmetrical: cigar driver of a slow truck passing a slower one on a long grade is but there is somebody else who dislikes it much more; and the the surfer dislikes having his board hit anybody in the head sport, and rarely reach accommodation with swimmers on how of the truck in front. Styles of behavior differ; surfers like to less conscious of who is behind him than the driver behind is water-skiers prefer dispersal and are engaged in a mobile be together and cluster somewhat in the absence of regulation: to share the water. Sometimes the problem is the other way around. It is

These several processes of separation, segregation, sharing, mixing, dispersal—sometimes even pursuit—have a feature in common. The consequences are aggregate but the decisions common. The consequences are aggregate but the decisions are exceedingly individual. The swimmer who avoids the part of the beach where the surfers are clustered, and the surfer who congregates where the surfboards are, are reacting individually to an environment that consists mainly of other individuals who are reacting likewise. The results can be unintended, even unnoticed. Non-smokers may concentrate in the least smoky railroad car; as that car becomes crowded, smokers, choosing less crowded cars, find themselves among smokers, whether they notice it or not, and less densely crowded, whether they appreciate it or not.

The more crucial phenomena are of course residential decisions and others, like occupational choice inter-city migration, school- and church-population, where the separating and mixing involve lasting associations that matter. The minor-

league players who eat lunch at Dodgertown have no cafeteria-line-mechanism to scramble their home addresses; and even if they were located at random, they would usually not be casually integrated, because mixed residential areas are few and the choice, for a black or for a white, is between living among blacks or living among whites—unless even that choice is restricted.

It is not easy to tell from the aggregate phenomenon just what the motives are behind the individual decisions, or how strong they are. The smoker on an airplane may not know that the person in front of him is sensitive to tobacco smoke; the water-skier might be willing to stay four hundred yards offshore if doing so didn't just leave a preferred strip to other skiers. The clustered men and women at that cocktail party may be bored and wish the hostess could shake things up, but without organization no one can do any good by hinself. And people who are happy to work where English and French are both spoken may find it uncomfortable if their own language falls to extreme minority status; and by withdrawing they only aggravate the situation that induced them to withdraw.

People who have to choose between polarized extremes—a white neighborhood or a black, a French-speaking club or one where English alone is spoken, a school with few whites or one with few blacks—will often choose in the way that reinforces the polarization. Doing so is no evidence that they prefer segregation, only that, if segregation exists and they have to choose between exclusive association, people elect like rather than unlike environments.

The dynamics are not always transparent. There are chain reactions, exaggerated perceptions, lagged responses, speculation on the future, and organized efforts that may succeed or fai. Three people of a particular group may break leases and move out of an apartment without being noticed, but if they do it the same week somebody will notice and comment. Other residents are then alerted to whether the whites or the blacks or the elderly, or the families with children or the families

without, are moving away, thereby generating the situation of minority status they thought they foresaw.

Some of the processes may be passive, systemic, unmotivated but nevertheless biased. If job vacancies are filled by word of mouth or apartments go to people who have acquaint-inces in the building, or if boys can marry only girls they know and can know only girls who speak their language, a biased communication system will preserve and enhance the prevailing homogeneities.

A Self-Forming Neighborhood Model

Some vivid dynamics can be generated by any reader with a half-hour to spare, a roll of pennies and a roll of dimes, a tabletop, a large sheet of paper, a spirit of scientific inquiry, or, lacking that spirit, a fondness for games.

Get a roll of pennies, a roll of dimes, a ruled sheet of paper divided into one-inch squares, preferably at least the size of a checkerboard (sixty-four squares in eight rows and eight columns) and find some device for selecting squares at random. We place dimes and pennies on some of the squares, and suppose them to represent the members of two homogeneous groups—men and women, blacks and whites, French-speaking and English-speaking, officers and enlisted men, students and faculty, surfers and swimmers, the well dressed and the poorly dressed, or any other dichotomy that is exhaustive and recognizable. We can spread them at random or put them in contrived patterns. We can use equal numbers of dimes and pennies or let one be a minority. And we can stipulate various rules for individual decision.

For example, we can postulate that every dime vants at least half its neighbors to be dimes, every penny wants a third of its neighbors to be pennies, and any dime or penny whose

immediate neighborhood does not meet these conditions gets up and moves. Then by inspection we locate the ones that are due to move, move them, keep on moving them if necessary and, when everybody on the board has settled down, book to see what pattern has emerged. (If the situation never "settles down," we look to see what kind of endless turbulence or cyclical activity our postulates have generated.)

Define each individual's neighborhood as the eight squares surrounding him; he is the center of a 3-by-3 neighborhood. He is content or discontent with his neighborhood according to the colors of the occupants of those eight surrounding squares, some of which may be empty. We furthermore suppose that, if he is discontent with the color of his own neighborhood, he moves to the nearest empty square that meets his demands.

As to the order of moves, we can begin with the discontents nearest the center of the board and let them move first, or start in the upper left and sweep downward to the right, or let the dimes move first and then the pennies; it usually turns out that the precise order is not crucial to the outcome.

Then we choose an overall ratio of pennes to dimes, the two colors being about equal or one of them being a 'minority.' There are two different ways we can distribute the dimes and the pennies. We can jut them in some prescribed pattern that we want to test, or we can spread them at random.

Start with equal numbers of dimes and pennies and suppose that the demands of both are "moderate"—each wants something more than one-third of his neighbors to be like himself. The number of neighbors that a coin can have will be anywhere from zero to eight. We make the following specifications. If a person has one reighbor, he must be the same color; of two neighbors, one must be his color; of three, four, or five neighbors, two must be his color; and of six, seven, or eight neighbors, he wants at least three.

It is possible to form a pattern that is regularly "integrated" that satisfies everybody. An alternating pattern does it (Figure 3), on condition that we take care of the corners.

Figure :

No one can move, except to a corner, because there are no other vacant cells; but no one wants to move. We now mix them up a little, and in the process empty some cells to make movement feasible.

There are 60 coins on the board. We remove 20, using a table of random digits, we then pick 5 empty squares at random and replace a cime or a penny with a 50-50 chance. The result is a board with 64 cells, 45 occupied and 19 blank Forty individuals are just where they were before we removed 20 neighbors and added 5 new ones. The left side of Figure 4 shows one such result, generated by exactly this process. The #'s are dimes and the O's are pennies; alternatively, the #'s speak French and the O's speak English, the #'s are black and the O's are write, the #'s are boys and the O's are girls, or whatever you please.

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Figure 4

The right side of Figure 4 identifies the individuals who are not content with their neighborhoods. Six #'; and three O's want to move; the rest are content as things stand. The pattern is still "integrated"; even the discontent are not without some neighbor; like themselves, and few among the content are without neighbors of opposite color. The general pattern is not strongly segregated in appearance. One is hard-put to block out #-neighborhoods or O-neighborhoods at this stage. The problem is to satisfy a fraction, 9 of 45, among the #'s and O's by letting them move somewhere among the 19 blank cells.

Anybody who moves leaves a blank cell that somebody can move into. Also, anybody who moves leaves behind a neighbor or two of his own color; and when he leaves a neighbor, his neighbor loses a neighbor and may become discontent. Anyone who moves gains neighbors like himself, adding a neighbor like them to their neighborhood but also adding one of opposite color to the unlike neighbors he acquires.

I cannot too strongly urge you to get the dimes and pennies and do it yourself. I can show you an outcome or two. A computer can do it for you a hundred times, testing variations in neighborhood demands, overall ratios, sizes of neighborhoods, and so forth. But there is nothing like tracing it through for yourself and seeing the thing work itself out. In an hour you can do it several times and experiment with different rules of behavior, sizes and shapes of boards, and (if you turn some of the coins heads and some tails) subgroups of dimes and pennies that make different demands on the color compositions of their neighborhoods.

Chain Reaction

What is instructive about the experiment is the "unraveling" process. Everybody who selects a new environment affects the environments of those he leaves and those he moves among. There is a chain reaction. It may be quickly damped,

with little mction, or it may go on and on and on with striking results. (The results of course are only suggestive, because few of us live in square cells on a checkerboard.)

One outcome for the situation depicted in Figure 4 is shown in Figure 5. It is "one outcome" because I have not explained exactly the order in which individuals moved. If the reader reproduces the experiment himself, he will get a slightly different configuration, but the general pattern will not be much different. Figure 6 is a replay from Figure 4, the only difference from Figure 5 being in the order of moves. It takes a few minutes to do the experiment again, and one quickly gets an impression of the kind of outcome to expect. Changing the neighborhood demands, or using twice as many dimes as pennies, will drastically affect the results; but for any given set of numbers and demands, the results are fairly stable.

All the people are content in Figures 5 and 6. And they are more segregated. This is more than just a visual impression: we can make a few comparisons. In Figure 4 the O's altogether had as many O's for neighbors as they had #'s some had more or less than the average, and 3 were discontent. For the #'s the ratio of #-neighbors to O-neighbors was 1:1, with a little colony of #'s in the upper left corner and 6 widely distributed discontents. After sorting themselves out in Figure 5, the average ratio of like to unlike neighbors for #'s and O's

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Figure 5

Figure 6

immediate neighborhood does not meet these conditions gets up and noves. Then by inspection we locate the ones that are due to move, move them, keep on moving them if necessary and, when everybody on the board has settled down, look to see what pattern has emerged. (If the situation never "settles down," we look to see what kind of endless turbulence or cyclical activity our postulates have generated.)

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As to the order of moves, we can begin with the discontents nearest the center of the board and let them move first or start in the upper left and sweep downward to the right, or let the dimes move first and then the pennies; it usually turns out that the precise order is not crucial to the outcome.

Then we choose an overall ratio of pennies to dimes, the two co.ors being about equal or one of them being a "minority." There are two different ways we can distribute the dimes and the pennies. We can put them in some prescribed pattern that we want to test, or we can spread them at random.

Start with equal numbers of dimes and pennies and suppose that the demands of both are "moderate"—each wants something more than one-third of his neighbors to be like himself. The number of neighbors that a coin can have will be anywhere from zero to eight. We make the following specifications. If a person has one neighbor, he must be the same color; of two neighbors, one must be his color; of three, four, or five neighbors, two must be his color; and of six, seven, or eight neighbors, he wants at least three.

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Figure 3

No one can move, except to a corner, because there are no other vacant cells; but no one wants to move. We now mix them up a little, and in the process empty some cells to make movement feasible.

There are 60 coins on the board. We remove 20, using a table of random digits; we then pick 5 empty squares at random and replace a dime or a penny with a 50-50 chance. The result is a board with 64 cells, 45 occupied and 19 blank. Forty individuals are just where they were before we removed 20 neighbors and added 5 new ones. The left side of Figure 4 shows one such result, generated by exactly this process. The #'s are dimes and the O's are pennies; alternatively, the #'s speak French and the O's speak English, the #'s are black and the O's are white, the #'s are boys and the O's are girls, or whatever you please.

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Figure 4

together was 2.3:1, more than double the original ratio. And it is about triple the ratio that any individual demanded! Figure 6 is even more extreme. The ratio of like to unlike neighbors is 2.8:1, nearly triple the starting ratio and four times the minimum demanded.

Another comparison is the number who had no opposite neighbors in Figure 4. Three were in that condition before people started moving; in Figure 5 there are 8 without neighbors of opposite color, and in Figure 6 there are 14.

What can we conclude from an exercise like this? We may at least be able to disprove a few notions that are themselves based on reasoning no more complicated than the checkerboard. Propositions beginning with "It stands to reason that..." can sometimes be discredited by exceedingly simple demonstrations that, though perhaps true, they do not exactly "stand to reason." We can at least persuade ourselves that certain mechanisms could work, and that observable aggregate phenomena could be compatible with types of "molecular movement" that do not closely resemble the aggregate outcomes that they determine.

There may be a few surprises. What happens if we raise the demands of one color and lower the demands of the other? Figure 7 shows typical results. Here we increased by one the number of like neighbors that a # demanded and decreased

Figure 7

by one the number that an O demanded, as compared with Figures 5 and 6. By mos: measures, "segregation" is about the same as in Figures 5 and 6. The difference is in population densities: the O's are spread out all over their territory, while the #'s are packed in tight. The reader will discover, if he actually gets those pennies and dimes and tries it for himself, that something similar would happen if the demands of the two colors were equal but one color outnumbered the other by two or three to one. The minority then tends to be noticeably more tightly packed. Perhaps from Figure 7 we could conclude that if surfers mind the presence of swimmers less than swimmers mind the presence of surfers, they will become almost completely separated, but the surfers will enjoy a greater expanse of water.

Is it "Segregated"?

The reader might try guessing what set of individual preferences led from Figure 4 to the pattern in Figure 8.

The ratio of like to unlike neighbors for all the #'s and O's together is slightly more than three to one; and there are 6 O's and 8 #'s that have no neighbors of opposite color. The result is evidently segregation; but, following a suggestion of my dictionary, we might say that the process is one of aggregation,

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Figure 8

because the rules of behavior ascribed both to #'s and to O's in Figure 8 were simply that each would move to acquire three neighbors of like color irrespective of the presence or absence of neighbors of opposite color. As an individua, motivation, this is quite different from the one that formed the patterns in Figures 5 and 6. But in the aggregate it may be hard to discent which motivation underlies the pattern, and the process, of segregated residence. And it matters!

The first impact of a display like this on a reader may be—unless he finds it irrelevant—discouragement. A moderate urge to avoid small-minority status may cause a rearly integrated pattern to unravel, and highly segregated neighborhoods to form. Even a deliberately arranged viable pattern, as in Figure 3, when buffeted by a little random motion, proves unstable and gives way to the separate neighborhoods of Figures 5 through 8. These then prove to be fairly immune to continued random burnover.

may be a note of hope. The underlying motivation can be far seeking when they collectively segregated themselves, there for those who deplore more segregation than people were it takes to keep things from unraveling is to be learned from 9 of the 45 individuals are motivated to move, and if we could once the process of separation has stabilized. In Figure 4 only restore such "integration" as would satisfy the individuals, Figure 4; the later figures indicate only how hard it may be to less extreme than the observable patterns of separation. What persuace them to stay everybody else would be all right. Figure 4 from outside, or how few individuals would need to cover how few individuals would need to be invited into Indeed the reader might exercise his own ingenuity to dismove. If two lonely #'s join a third lonely #, none of them is unless assured that the third will arrive, and without some conlonely anymore, but the first wil. not move to the second be relocated in Figure 4, to keep anybody from wanting to cert or regulation, each will go join some larger cluster, per-For those who deplore segregation, however, and especially

haps abandoning some nearby lonely neighbor in the process and surely helping to outnumber the opposite color at their points of arrival.

The Bounded-Neighborhood Model

Turn now to a different model, and change the definition of "neighborhood." Instead of everyone's defining his neighborhood by reference to his own location, there is a common definition of the neighborhood and its boundaries. A person is either inside it or outside. Everyone is concerned about the color ratio within the neighborhood but not with the arrangement of colors within the neighborhood. "Residence" can therefore just as well be interpreted as membership or participation in a jab, office, university, church, voting bloc, restaurant, or hospital.

In this model there is one particular area that everybody, black or white, prefers to its alternatives. He will live in it unless the percentage of residents of opposite color exceeds some limit. Each person, black or white, has his own limit. ("Tclerance," I shall occasionally call it.) If a person's limit is exceeded in this area he will go someplace else—a place, presumably, where his own color predominates or where color does not matter.

"Tolerance," it should be noticed, is a comparative measure. And it is specific to this location. Whites who appear, in this location, to be less tolerant of blacks than other whites may be merely more tolerant of the alternative locations.

Evidently the limiting ratios must be compatible for some blacks and some whites—as percentages they must add to at least 100—or no contented mixture of any whites and blacks is possible. Evidently, too, if nobody can tolerate extreme ratios, an area initially occupied by one color alone would remain so.